

Bargaining Theory

Abhinav Muthoo
<http://www.essex.ac.uk/economics/people/staff/muthoo.shtm>

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Bargaining in Game Theory

◆ Rubinstein Model:

In reality:
Offer at time $t = f(r_A, r_B, t)$
Is it necessary?
Is it rational? (What *is* rational?)

◆ A's payoff x_A drops as time goes by
A's Payoff = $x_A \exp(-r_A t \Delta)$

◆ Important Assumptions:
– Both players rational
– Both players know *everything*

◆ Equilibrium solution for A:
$$\mu_A = (1 - \delta_B) / (1 - \delta_A \delta_B)$$
 where $\delta_i = \exp(-r_i \Delta)$

Optimal offer:
 $x_A = \mu_A$
at $t=0$

Notice:
No time t here

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Bargaining is a branch of Game Theory

◆ Game theory is a mathematical framework
– A set of methods and tools
– For studying strategic situations

◆ Bargaining games constitute the best/classic class of games
– It involves conflicts (we both want a bigger share)
– It need cooperation (we both need a deal asap)

◆ Repeated Games is another big class of games

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Terminology in bargaining theory

◆ Optimal – doing what is best for oneself
– In bargaining, what is best for me depends on what the other player does


◆ Subgame – now and at any point in the future

◆ Subgame Perfect Equilibrium (SPE)
– Each player deploys a strategy that is best for her at each and every subgame
– Optimal strategy by both players

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Iterative Prisoner's Dilemma

Axelrod's experiments
Tit-for-tat



Prisoner's Dilemma

Payoffs		Player A	
		Cooperate	Defect
Player B	Co-operate	1 / 1	0 / 4
	Defect	4 / 0	2 / 2

- What's the optimal decision for A (or B)?
- What if this game is repeated?

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Iterated Prisoner's Dilemma (IPD)

- ♦ Axelrod organized two tournaments in 1980
 - Round one: 14 entries
 - Round two: 62 entries from 6 countries
- ♦ Tit-for-Tat was the winner in both runs
 - Start by cooperation
 - Then follow whatever the opponent did last round
- ♦ GRIM is an alternative local optimum
 - Like Tit-for-Tat, except being unforgiving

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Trading Agents Competition for E-Commerce



Maria Fasli

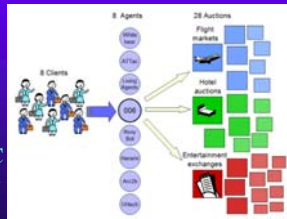
<http://cswww.essex.ac.uk/staff/mfasli>



Trading Agents Competition (TAC)

Classic Game (*Thalis*)

- Simultaneous auctions with substitutable and interrelated goods
- Dynamic bid configuration depending on historical data, current state and projected state
- Application of *Strategic Demand Reduction*
- Domain-specific heuristics
- 3rd and 4th positions in TAC 2003 and 2004 respectively



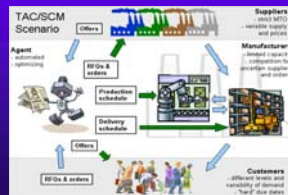
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TAC Work at Essex

Supply Chain Management Game (*Socrates*)

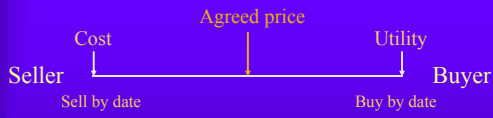
- An agent acts as a reverse auctioneer with the suppliers in multi-attribute auctions with substitutable and interrelated goods. Suppliers use a reputation mechanism and their delivery may be partial or complete
- Dynamic scheduling for production and delivery
- Ordering strategy and factory utilisation are interdependent and crucial
- ICEC-03: 7th position



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Local Constraint Optimisation



- ◆ Every agent is self-centred
- ◆ Agents constrain each other
- ◆ The simplest form of local constraint satisfaction / optimisation above
 - All deeper research depends on strategy in this problem

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Game Theory Hall of Fame

1994
Nobel
Prize



John Harsanyi



John Nash



Reinhard Selten

2005
Nobel
Prize



Robert Aumann



Thomas Schelling



1994 Nobel Economic Prize Winners



John Harsanyi
(Berkeley)
Incomplete information



John Forbes Nash
(Princeton)
Non-cooperative games



Reinhard Selten (Bonn)
Bounded rationality
(after Herbert Simon)
Experimental economics

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1978 Nobel Economic Prize Winner

- ◆ Artificial intelligence
- ◆ “For his pioneering research into the decision-making process within economic organizations”
- ◆ “*The social sciences, I thought, needed the same kind of rigor and the same mathematical underpinnings that had made the “hard” sciences so brilliantly successful.*”
- ◆ Bounded Rationality
 - *A Behavioral model of Rational Choice* 1957



Herbert Simon (CMU)

Artificial intelligence

Sources: <http://nobelprize.org/economics/laureates/1978/> <http://nobelprize.org/economics/laureates/1978/simon-autobio.html>

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2005 Nobel Economic Prizes Winners

- ◆ Robert J. Aumann, and Thomas C. Schelling won 2005’s Noel memorial prize in economic sciences
- ◆ For having enhanced our understanding of conflict and cooperation through game-theory analysis



Robert J. Aumann

75

Thomas C. Schelling

84

Source: <http://www.msnbc.msn.com/id/9649575/> Updated: 2:49 p.m. ET Oct. 10, 2005

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Robert J. Aumann

Winner of 2005 Nobel Economic Prize

- ◆ Born 1930
- ◆ Hebrew Univ of Jerusalem & US National Academy of Sciences
- ◆ “Producer of Game Theory” (Schelling)
- ◆ Repeated games
- ◆ Defined “*Correlated Equilibrium*”
 - Uncertainty not random
 - But depend on info on opponent
- ◆ Common knowledge



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Thomas C. Schelling

Winner of 2005 Nobel Economic Prize



- ◆ Born 1921
- ◆ University of Maryland
- ◆ “User of Game Theory” (Schelling)
- ◆ Book “The Strategy of Conflict” 1960
 - Bargaining theory and strategic behavior
- ◆ “Book Arms and Influence” 1966
 - foreign affairs, national security, nuclear strategy, ...
- ◆ Paper “Dynamic models of segregation” 1971
 - Small preference to one’s neighbour → segregation

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