

Course EE212

University of Essex

Part 1, Section 6

Evaluation experiment design and statistics

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DESIGNING EXPERIMENTS - Overview

 An experiment is a sequence of tests

- Choosing variables and conditions to cover the area of interest trying to exclude distracting or unnecessary variables
- Selecting subjects
 - to represent the intended users
- Designing the procedure explaining the experiment to trial users, with consistency allowing for learning effects by altering the test sequence
 - constructing a 'statistically-useful' sequence of tests
 - capturing user responses or reactions in words, numbers or actions

EVALUATION EXPERIMENTS - aims and techniques

Aims

construct experiment that is simple and unbiased these aims are often *conflicting*

Techniques

replication balancing randomisation blocking structure

SIMPLE EVALUATION - example (1)

Experiment - for a text-editing application

suppose we want to compare the speed of positioning the edit cursor, using either cursor keys or mouse 'move and click'

one variable, that can take two values (treatments): keys or mouse

Method

measure the cumulative time taken to position the cursor correctly use same task (text and original position of cursor) for each test, otherwise variation in task will affect the measured time

Treatment	Time(secs)
А	45
В	28

one trial user uses treatment A - keys then treatment B - mouse

what is wrong ... learning effect

EVALUATION EXPERIMENTS - example (2)

Add another trial user - replication
 each user experiences one test - no learning effect is possible
 first user tries treatment A, second user tries treatment B

Subject	Treatment Time(secs)		
1	А	40	
2	В	30	

mouse (treatment B) still seems faster

 Fixed one problem, but introduced another problem ... measured difference might be due to differences between people maybe user 2 has faster reactions or movements than user 1 maybe user 1 has little experience of using a keyboard

EVALUATION EXPERIMENTS - example (3)

 Add another pair (or many pairs) of trial users reduce (average-out) the variation due to the different users first user tries treatment A, second user tries treatment B

Subject	Treatment Time(secs)	
1	А	40
2	В	30
3	А	38
4	В	32

average of treatment A = 39 average of treatment B = 31 difference A_{AV} and B_{AV} = 8 difference between users = 2 (for same treatment) mouse seems *truly* faster

 Measured difference is much larger than user variation so results form a reasonable conclusion, without more analysis not always like that ...

EVALUATION EXPERIMENTS

- observations (about observations)
- A single measurement (observation)

- of each treatment is not sufficient ... it does not allow independent assessment of treatment variability
- What if the difference between treatments is small ? increase the number of trial users

variation due to N users typically changes as N $^{-0.5}$ use statistical methods to decide if measured difference is significant

- Experiments with large numbers of subjects suppose there are 64 trial users, and each test takes 5 minutes total time for experiment is at least 5 hours 20 minutes that's enough time for the room to get hot or stuffy, enough time for the amount of daylight to change, etc.
- Balance the sequence of treatments not 'all A' then 'all B' randomise the test sequence - use tables of random numbers

SENSITIVE EXPERIMENTS - to measure small differences

Is there a better way ...

than adding more and more trial users ? yes - use each trial user more than once

• Earlier examples

all used the 'between subjects' method of experimental design each subject tested one treatment measured differences were between treatments, but also between users

• 'Within subjects' design - more efficient use of trial users each user tests all of the treatments

advantage is reduced variability due to different users - more precision each user acts as their own 'control' or reference case

disadvantage is *much* greater opportunity for learning effects to occur total time for the experiment does not change

SENSITIVE EXPERIMENTS - 'within subjects' design method

Blocking structure

where each user contributes a block (here, a row) of results randomly allocate trial users to blocks

.	Trea	Period 2 tment	Subject
Subject	Α	В	average
1	40	28	34
2	45	30	37.5
3	38	27	32.5
4	36	32	34
Treatment average	39.75	29.25	34.5 Over avera

possible to calculate : averages for each treatment averages for each user these are independent ... greater precision in measuring both treatment and user effects *learning* effect is a

serious problem

One further improvement to the design is needed ... balance the treatment sequence

SENSITIVE EXPERIMENTS - 'within subjects' design method

 Alternate the order of treatments in different blocks known as 'Latin Squares' design - fully balanced, randomised block there are as many users as treatments as periods

Subject	Period 1	Period 2	Subject average
1	A ₄₁	В ₂₇	34
2	B ₃₁	A ₄₄	37.5
3	A ₃₉	В ₂₆	32.5
4	В ₃₃	A ₃₅	34
Treatment	averages:	A - 39.75	34.5 Ove

1 - 36 2 - 33

Period averages:

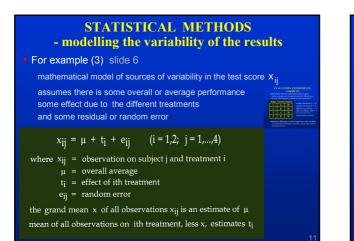
users are the 'blocking factor' on the rows

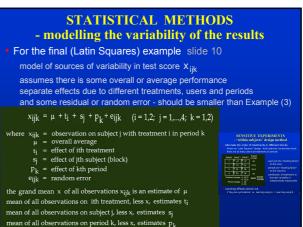
periods are 'blocking factor' on the columns

contribution of treatments to the total variability is independently measurable

Learning effects cancel out if they are symmetrical ie. learning using A = learning using B

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STATISTICAL METHODS - formal terminology

In comparative experiments

to estimate the probability that the differences measured in the experiment might have happened by chance

if probability is low enough, result is said to be *significant* at that level eg. if result is significant at 5% level, then only 1 in 20 chance that this result happened by chance

Use of hypotheses

null hypothesis assumes there is no difference between treatments alternative hypothesis assumes some difference between treatments assume null hypothesis is true, then look for significant differences if found reject null hypothesis and accept alternative hypothesis

STATISTICAL METHODS - data distributions and significance tests

Method used depends on :

number of treatments assumptions about the nature, and internal dependencies, of the data

Distribution of experimental data

often assume random processes, so data follows normal distribution (Gaussian)

Tests for statistical significance

if there are two treatments - 't-test' more than two treatments - 'ANOVA' (analysis of variance), 'F-test' these only test the null hypothesis, if any significance is found then further tests are used to establish which variable is significant -'multiple t-test' and 'Tukey's test' (Wetherill, 1981)

Scales of Measurement

Nominal

Categories, such as colours (red, blue), gender, marital status

Ordinal

Rank order, e.g. 1st, 2nd and 3rd as in horse racing

Interval

Like ordinal, but difference between 1^{st} and 2^{nd} is the same as distance between 2^{nd} and 3rd

Ratio

Such as mass, length, age

 Reference: S. S. Stevens, On the theory of scales of measurement, Science 103, 1946, pp667-680

STATISTICAL METHODS - other distributions and issues

 Normal distribution of experimental data is not always true

• Frequency measurements eg. number of users in a category - follow Poisson distribution

Ranking measurements

eg. ratings in questionnaire answers use Mann-Whitney / Wilcoxon tests (Gibbons, 1971)

Statistical significance

is a mathematical idea ...

a non-significant difference is *not* the same as proof of no difference just means that the experimental conditions found no difference significant difference is not *necessarily* interesting or useful difference

EVALUATION - summary

 Effective evaluation is not easy classic mistakes are easy to make but good evaluations save time / money - avoid rework after production

 Evaluate early and often use simple methods at first, more complex methods later in design variety of opinion, from experts and several kinds of users, is valuable

Trial users

think about potential bias (intended or not) when you select them

The design of evaluations is important advance planning, for all kinds of evaluation, is essential writing good questionnaires, and holding useful interviews, needs care sequence of tests, and organisation of arithmetic, makes big difference statistical analysis is powerful, but significant results not always useful